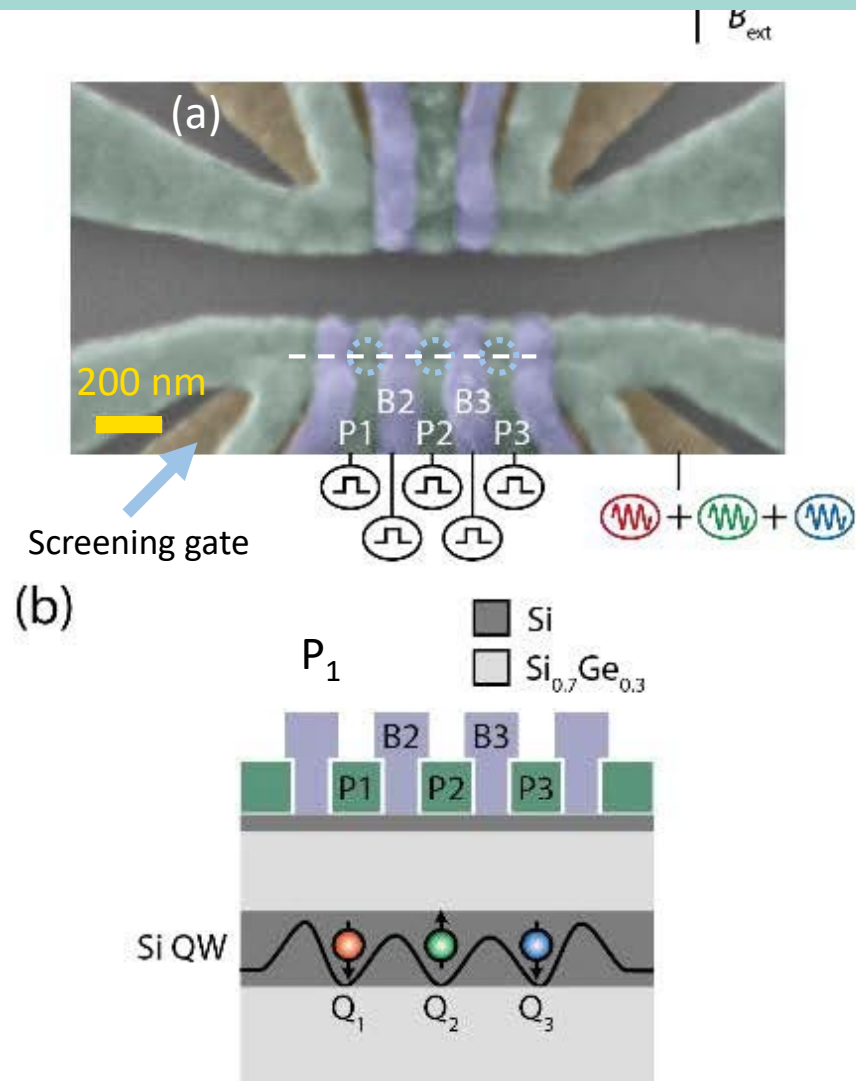


Quantum tomography of an entangled three-spin state in silicon

Kenta Takeda, Akito Noiri, Takashi Nakajima, Jun Yoneda, Takashi Kobayashi, Seigo Tarucha

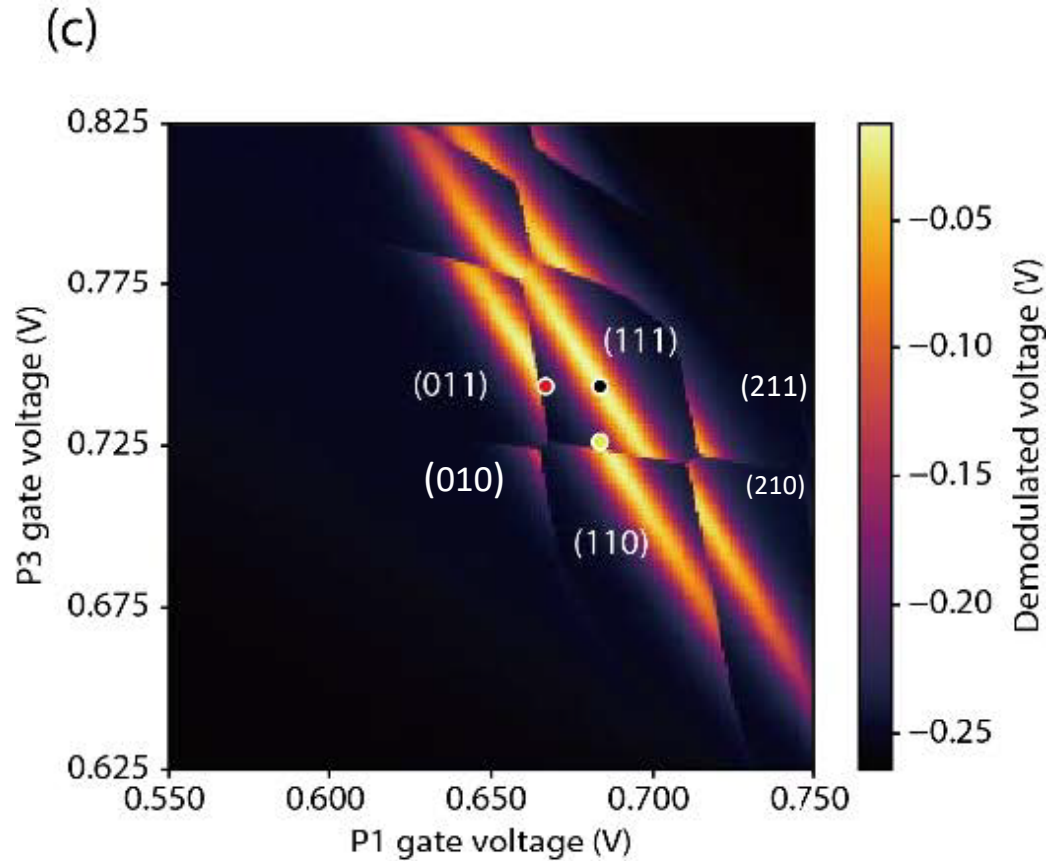
Pierre Chevalier Kwon
30.10.2020

Device architecture



- Si/SiGe heterostructure (2DEG)
- 3 Al layers
- Dilution refrigerator: $T_e \sim 40$ mK
- Inplane magnetic field: $B_{\text{ext}} \sim 0.5$ T + a magnetic field gradient (in and outplane) made by a cobalt micro-magnet (on top of the QDs)
- (Radio-frequency) Sensor QD (at top)

Charge stability diagram



- The background signal variation is due to the sensor dot Coulomb oscillation.
- Red point ● is Q_1 readout/initialization point
- Yellow point ● is Q_2 and Q_3 readout/initialization point
- Black point ● is the qubit manipulation point

Measurement sequence: Basic operations

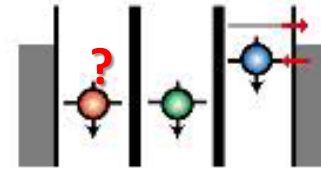
① Initialize Q_3



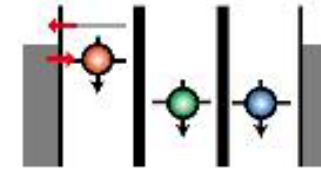
② SWAP Q_3 and Q_2



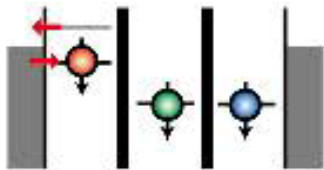
③ Initialize Q_3



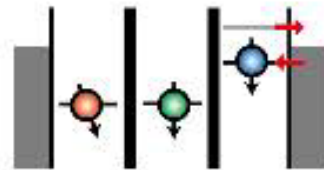
④ Initialize Q_1



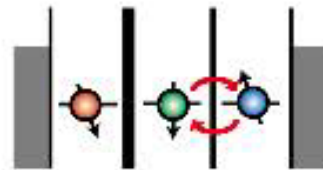
⑨ Readout Q_1



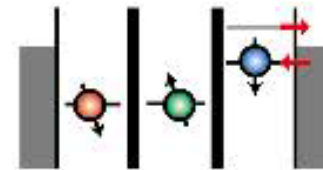
⑧ Readout Q_2 via Q_3



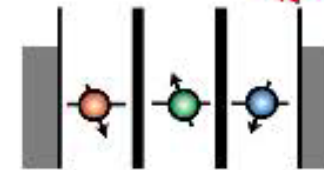
⑦ SWAP Q_3 and Q_2



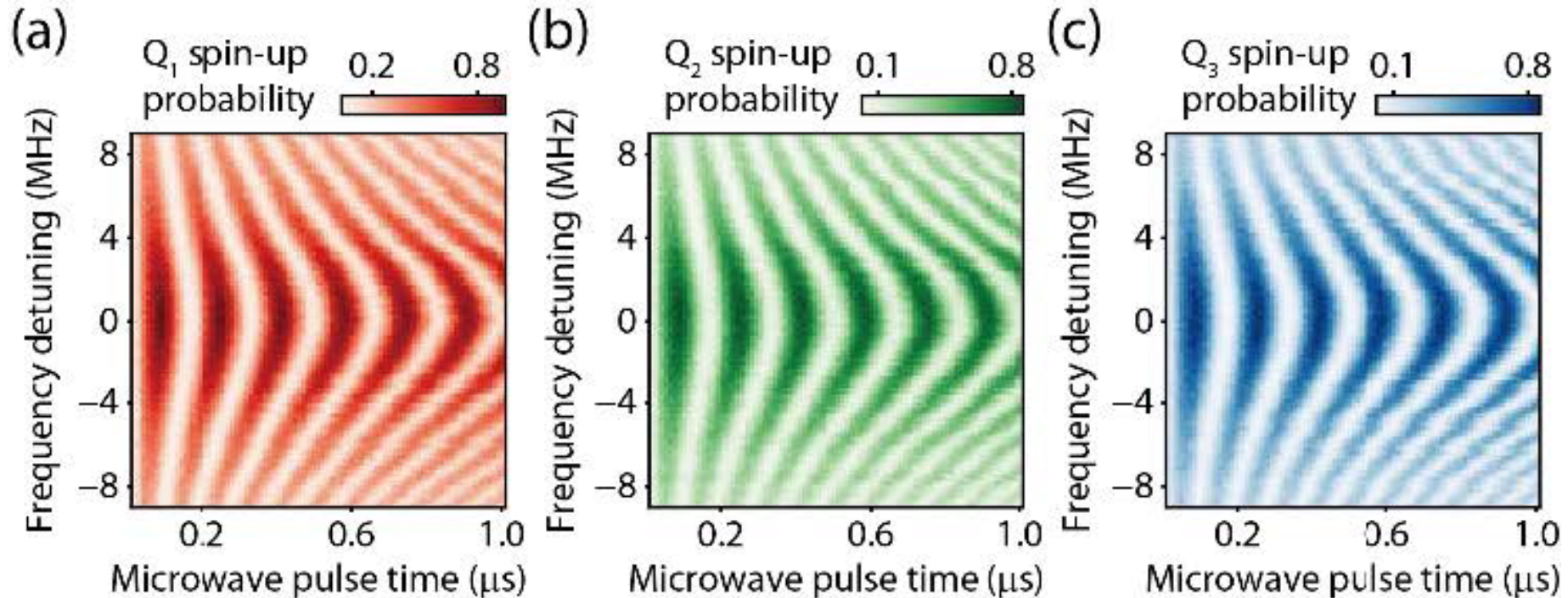
⑥ Readout Q_3



⑤ Manipulation (EDSR)

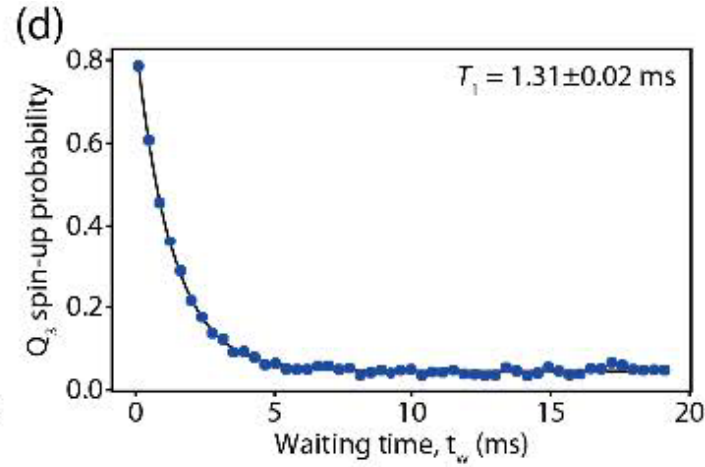
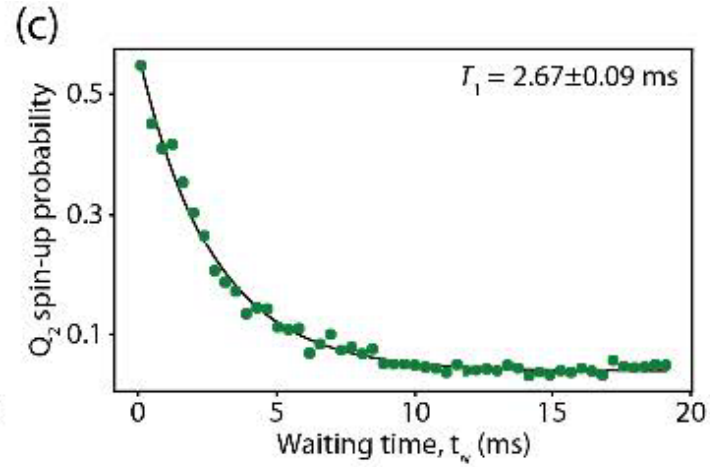
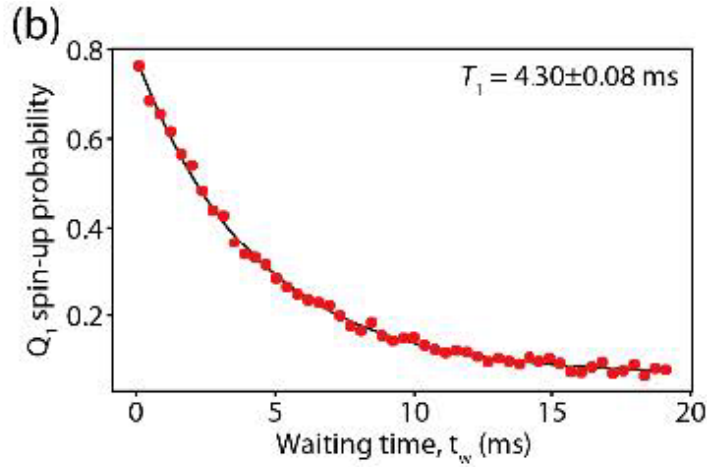
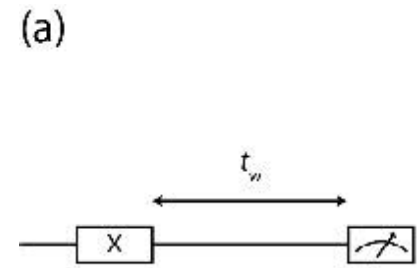


Rabi chevron oscillations of each qubit



- The frequency offsets are 17789.15 MHz (Q_1), 18224.5 MHz (Q_2), and 18747.7 MHz (Q_3).
 - So $\delta E_{12} \approx 435.4$ MHz and $\delta E_{23} \approx 523.2$ MHz
- $f_{\text{rabi}} \approx 6$ MHz

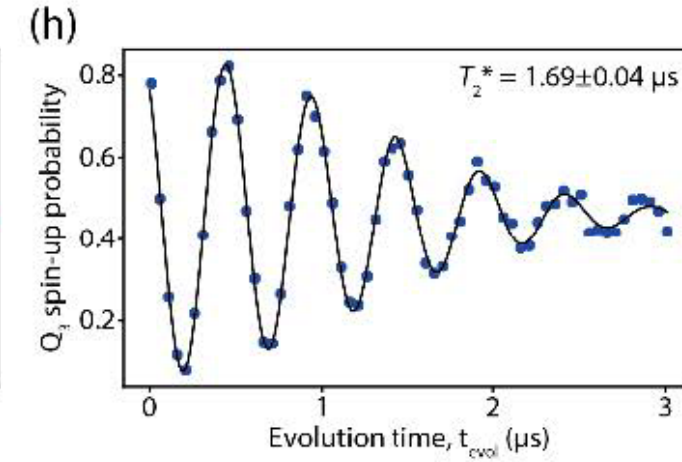
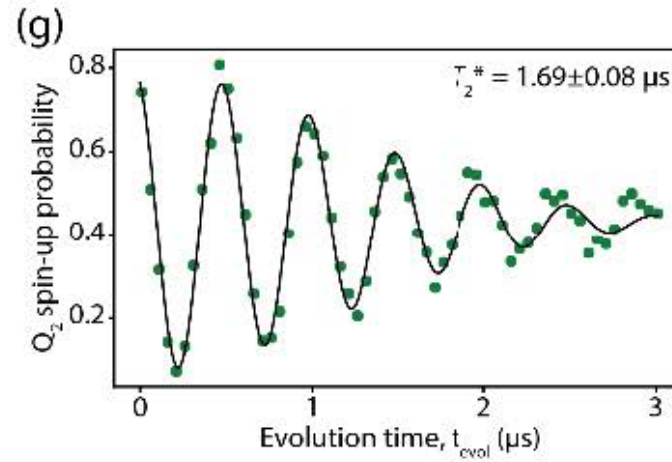
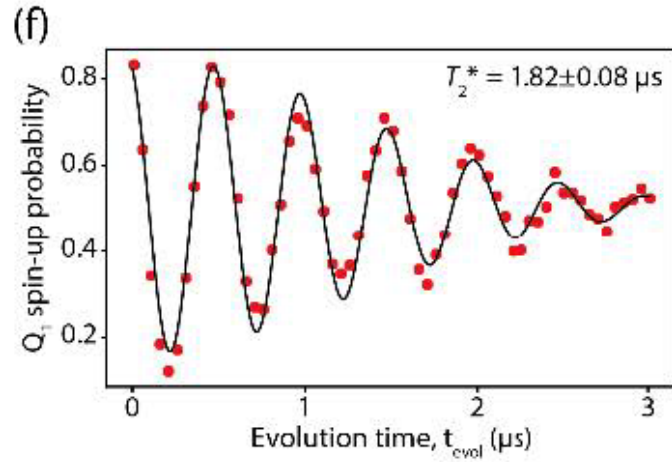
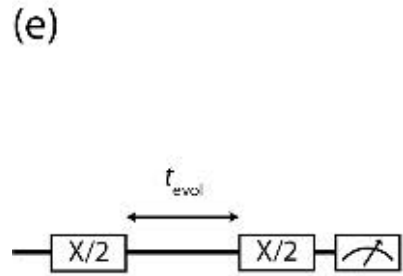
T_1 measurements



- $T_1(Q_1) = 4,30 \pm 0,08$ ms
- $T_1(Q_2) = 2,67 \pm 0,09$ ms
- $T_1(Q_3) = 1,31 \pm 0,02$ ms

- long enough to perform single-shot spin readout
- shorter than typically values for electron spins in silicon (probably due to spin-valley mixing)

Ramsey interferometry measurements

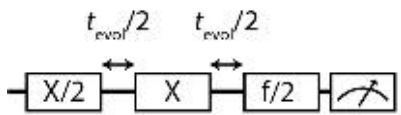


- $T_2^*(Q_1) = 1,82 \pm 0,08 \mu\text{s}$
- $T_2^*(Q_2) = 1,69 \pm 0,08 \mu\text{s}$
- $T_2^*(Q_3) = 1,69 \pm 0,01 \mu\text{s}$

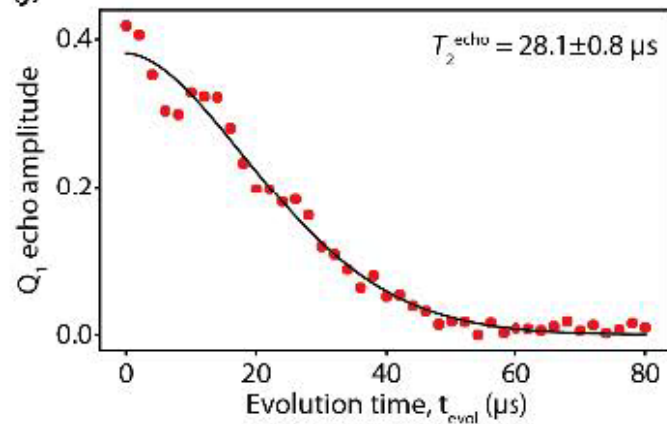
- Typical value for natural silicon spin-1/2 qubits
- Probably limited by the fluctuation of 4.7% ²⁹Si nuclear spins in natural silicon

Hahn echo measurements

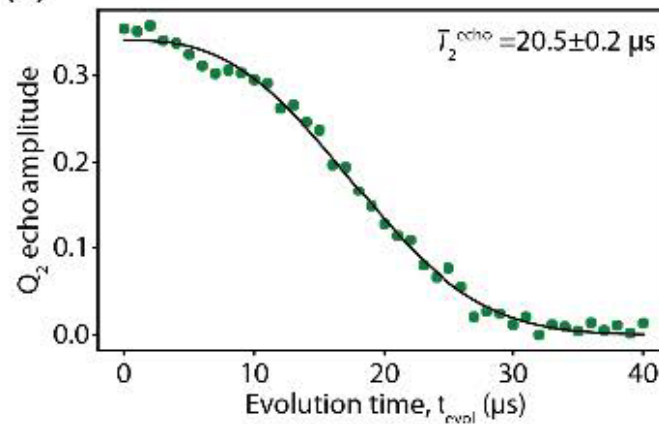
(i)



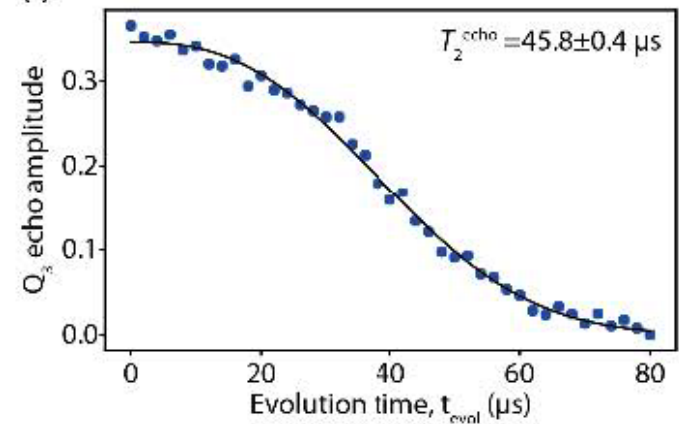
(j)



(k)



(l)

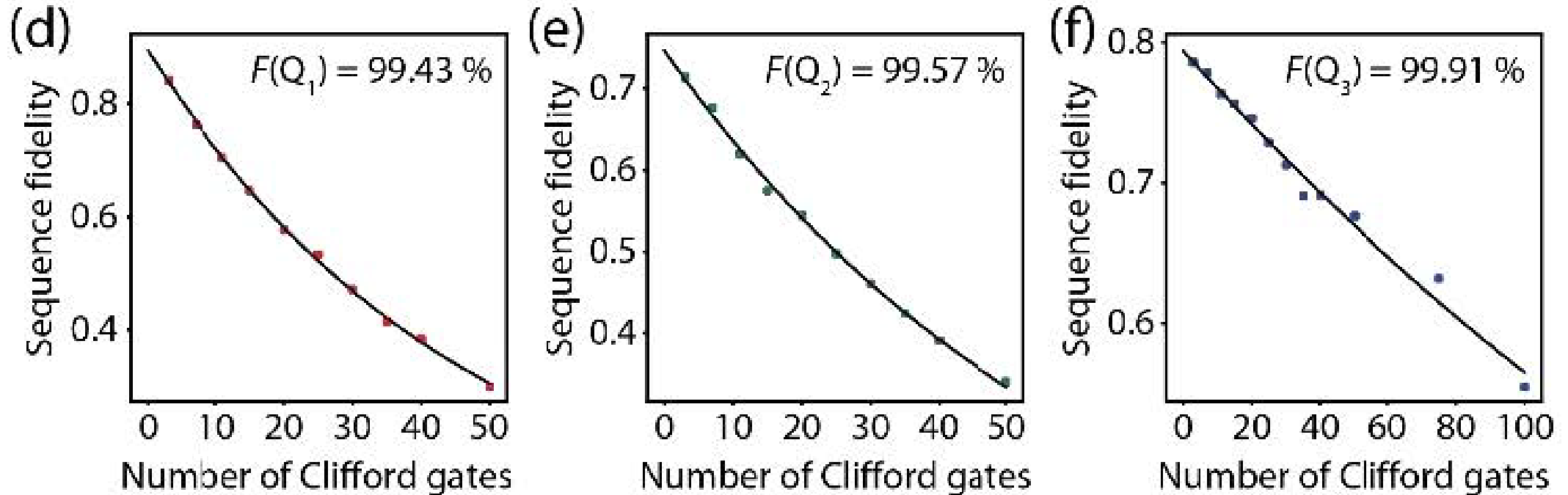


- $T_2^{\text{echo}}(Q_1) = 28,08 \pm 0,08 \mu\text{s}$
- $T_2^{\text{echo}}(Q_2) = 20,5 \pm 0,02 \mu\text{s}$
- $T_2^{\text{echo}}(Q_3) = 45,8 \pm 0,04 \mu\text{s}$

- Hahn echo extends the dephasing times to ~ 1 order of magnitude

Single-qubit control fidelities

Clifford-based randomized benchmarking



- high enough to perform the quantum state tomography measurements

Goal of this experiment

- We want to make an (useful) entangled 3 qubits state

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=>Let's make a GHZ (GigaHertz Greenberger–Horne–Zeilinger) state (because it is useful for quantum error correction)

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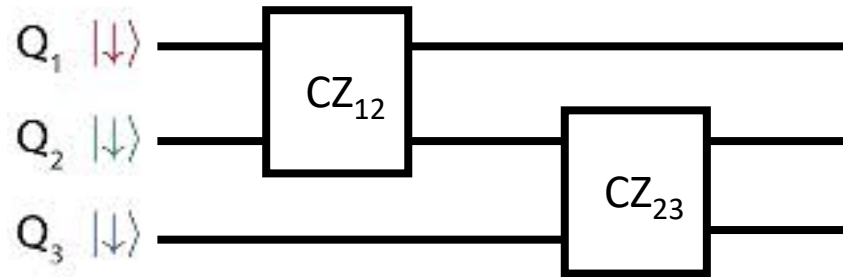
=> Let's characterize it by quantum state tomography

How to make GHZ state?

- Exchange coupling for 2 neighbouring qubits + Zeeman gradient (thanks to the micro-magnet) => CZ gates

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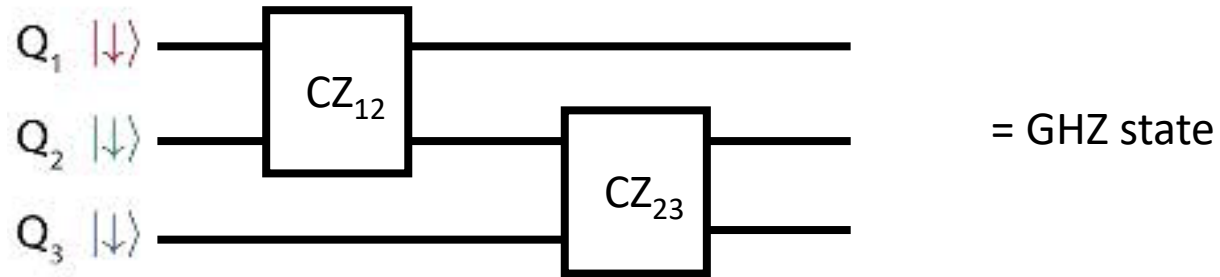
- Exchange coupling for 2 neighbouring qubits + Zeeman gradient (thanks to the micro-magnet) => CZ gates
- In theory:



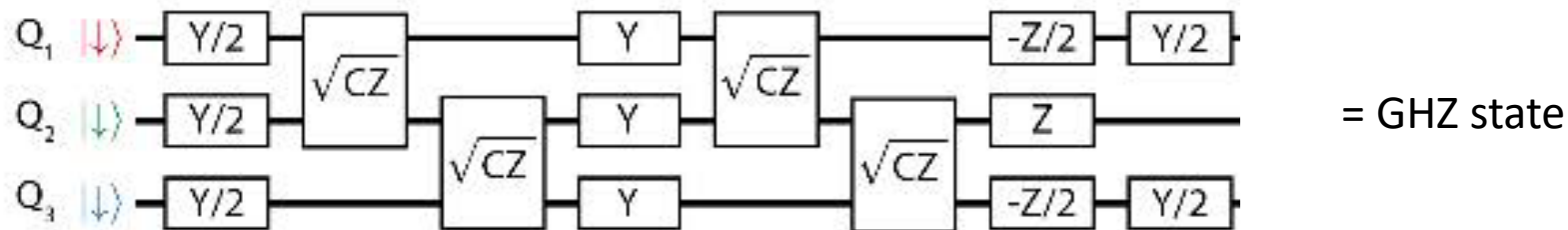
= GHZ state

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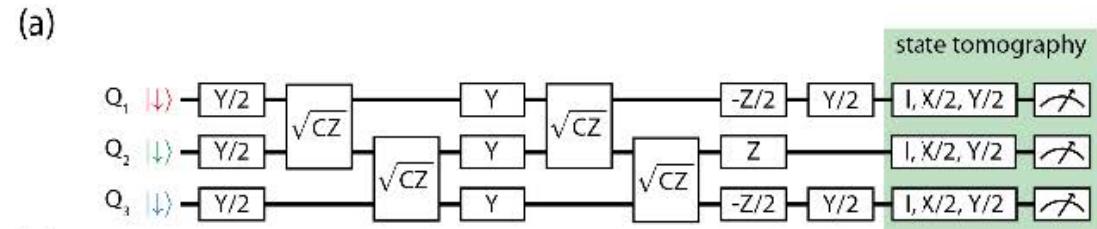
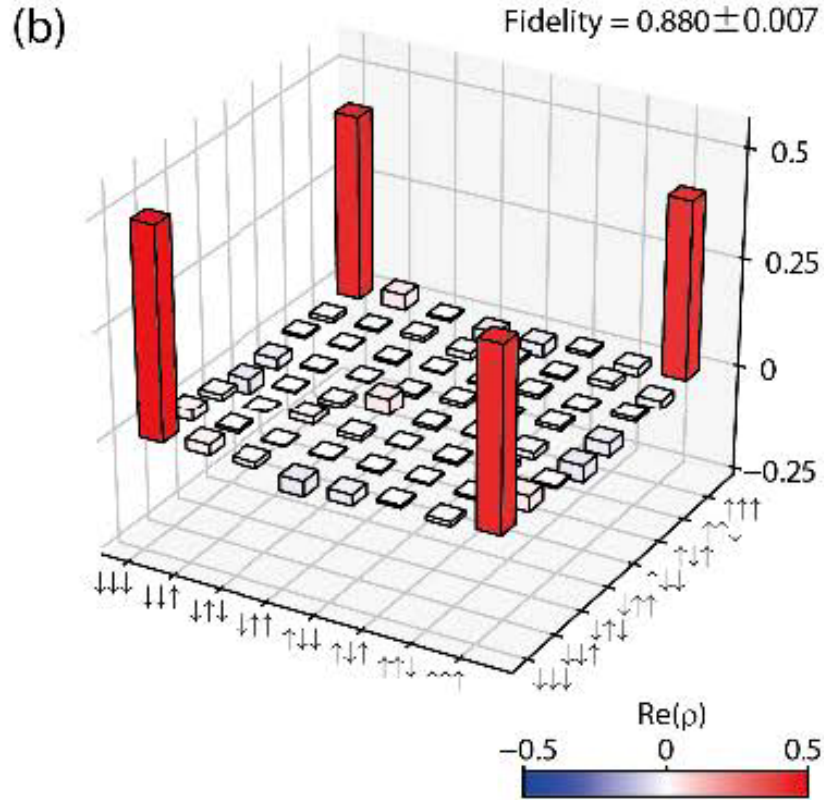


- But. to avoid low-frequency noise. it becomes:



=> It is same principle as Hahn echo

State tomography



- measured density matrix \Rightarrow Fidelity $F_{\text{GHZ}} = \langle \text{GHZ} | \rho | \text{GHZ} \rangle = 0.880 \pm 0.007$
- Same order of magnitude that the first time this state was realized (with superconducting device)

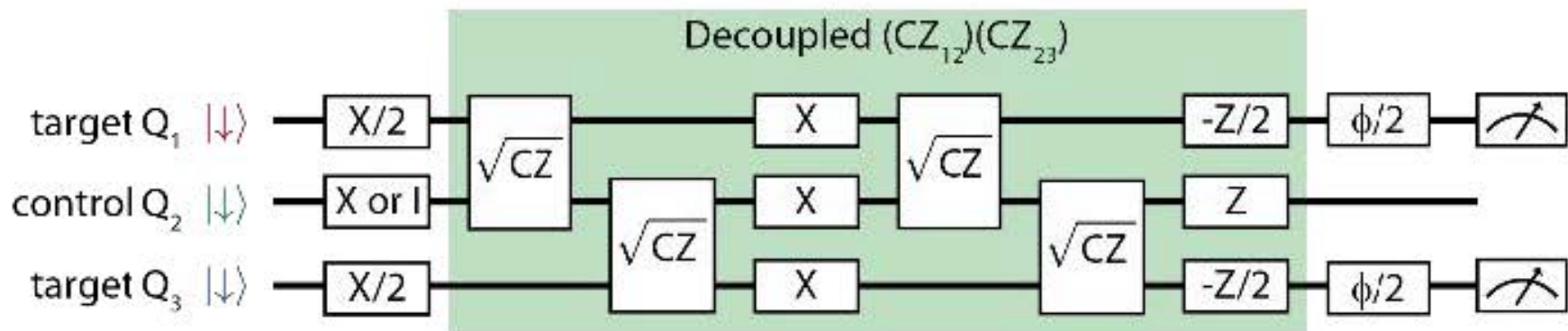
Conclusion

- Shown operation of a three-qubit device in silicon
 - Generation and measurement of a three-qubit GHZ state
- Characterized by quantum state tomography
 - “high” fidelity
- Overall, result that can lead of multi-qubit algorithms such as quantum error correction in scalable silicon-based quantum computing devices.

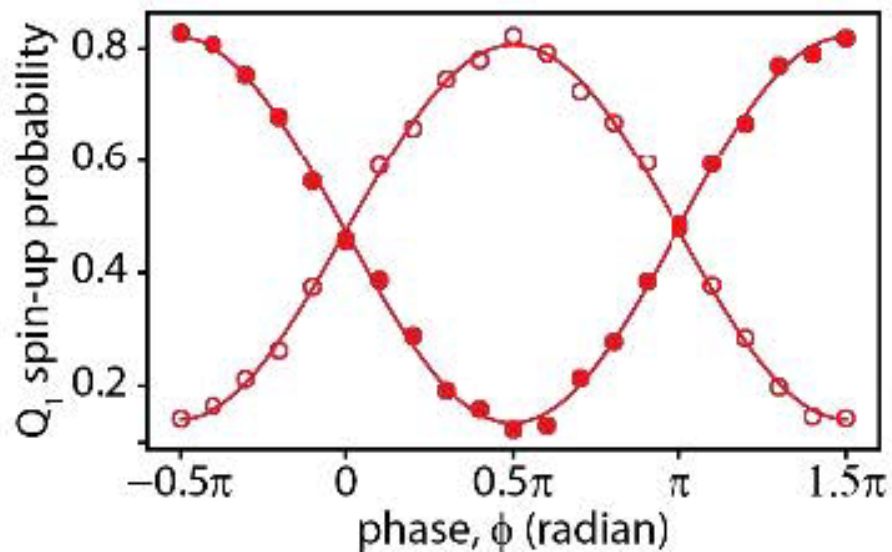
Thank you for your attention!

Tuning of the CZ gates

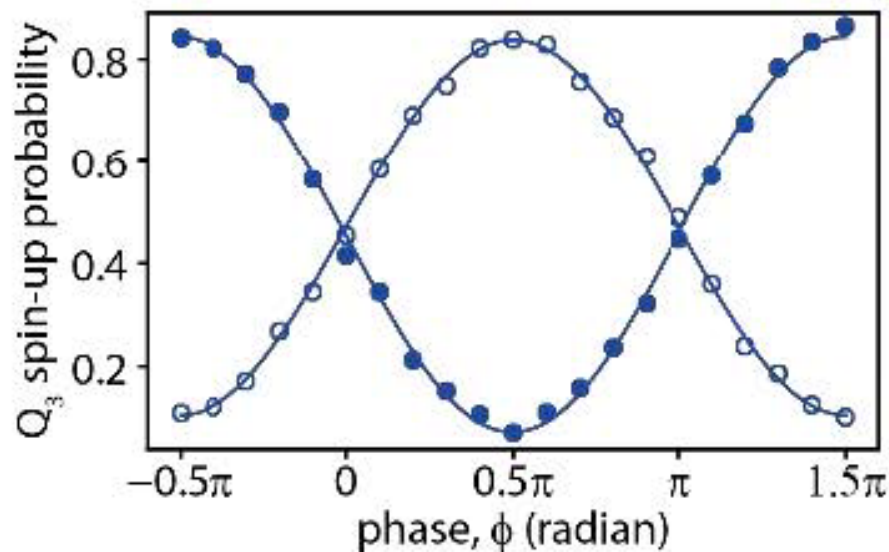
(g)



(h)



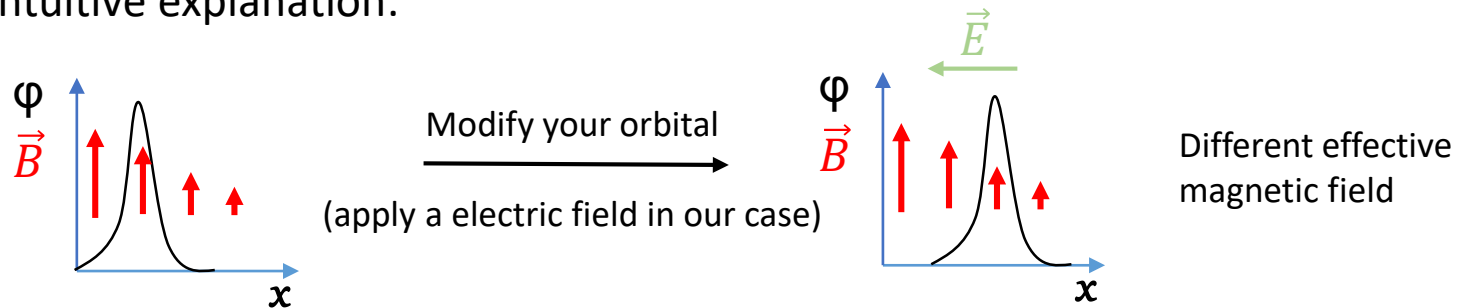
(i)



Electric-Dipole Spin Resonance (EDSR)

- Gradient of B outplane (B_{outplane}) is used to couple electron's spin and orbital degrees of freedom (in other words: allows the ESR)

Intuitive explanation:



- Gradient inplane is used to give different Larmor frequencies for spin in each QD. Hence, we can selectively rotate S_R or S_L (resonant frequency $\propto B_{\text{inplane}}$)
- Typical values*: $\delta B_{\text{outplane}} > 0.8 \text{ mT/nm}$ and $\Delta B_{\text{inplane}} > 18 \text{ mT}$

*Yasuhiro Tokura, Wilfred G. van der Wiel, Toshiaki Obata, and Seigo Tarucha, Phys. Rev. Lett. 96, 047202 (2006).