

Group Seminar

June 14, 2019

Zumbühl Group

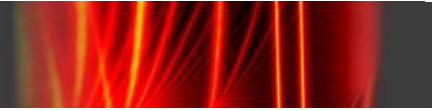
Henok Weldeyesus

Aharonov–Bohm interference of fractional quantum Hall edge modes

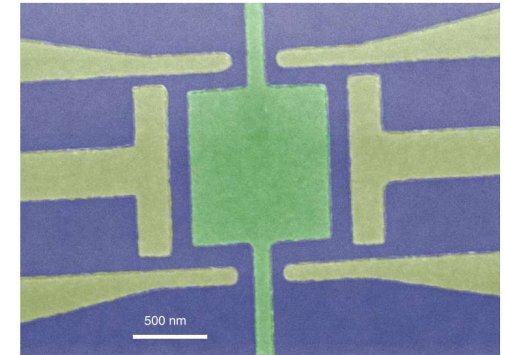
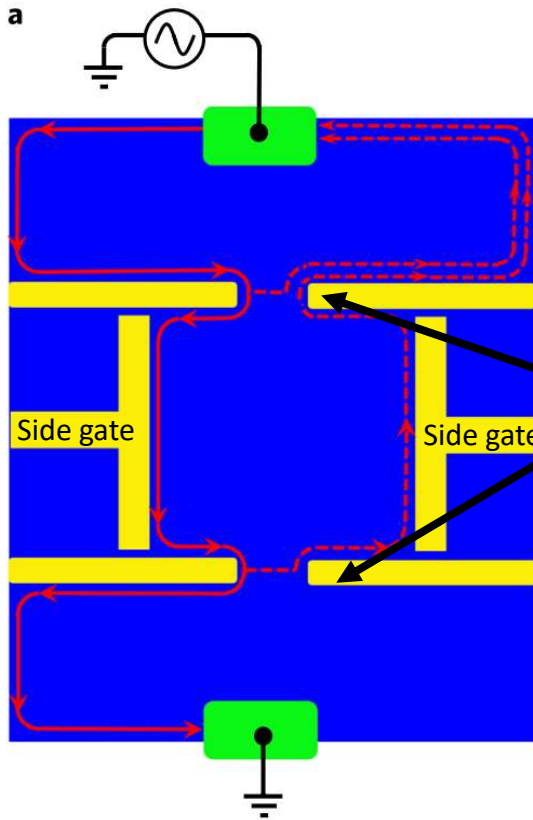
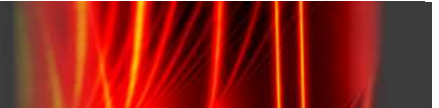
J. Nakamura^{1,2}, S. Fallahi^{1,2}, H. Sahasrabudhe¹ , R. Rahman³ , S. Liang^{1,2}, G. C. Gardner^{2,4} and M. J. Manfra^{1,2,3,4,5*} 

The braiding statistics of certain fractional quantum Hall states can be probed via interferometry of their edge states. Practical difficulties—including loss of phase coherence—make this a challenging task. We demonstrate the operation of a small Fabry–Perot interferometer in which highly coherent Aharonov–Bohm oscillations are observed in the integer and fractional quantum Hall regimes. Careful design of the heterostructure suppresses Coulomb effects and promotes strong phase coherence. We characterize the coherency of edge-mode interference by the energy scale for thermal damping and determine the velocities of the inner and outer edge modes independently via selective backscattering of edge modes originating in the $N = 0, 1, 2$ Landau levels. We also observe clear Aharonov–Bohm oscillations at fractional filling factors $\nu = 2/3$ and $\nu = 1/3$, which indicates that our device architecture provides a platform for measurement of anyonic braiding statistics.

- Aharonov-Bohm interference
- Interferometer Regimes
- Device Properties
- Results
 - Fractional edge state interferometry
 - Edge state velocities



- Investigation of (fractional) quantum Hall effect
 - Edge state velocities
 - (non)-Abelian fractional statistics
- Problems with Aharonov-Bohm interferometry
 - Small coherence length of fractional edge states requires small interference area
 - Small interference Area causes larger coulomb charging energy



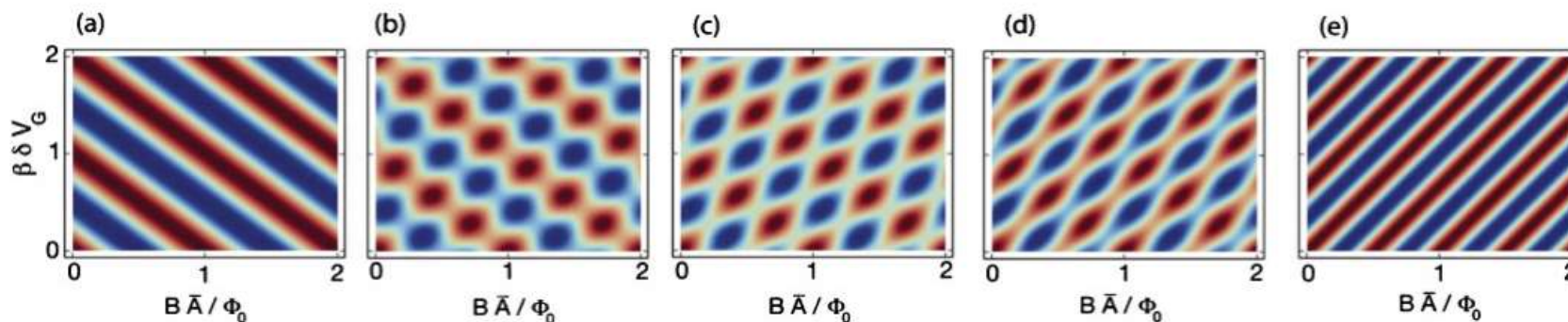
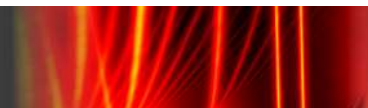
Quantum point contact (QPC)

AB-interference at weak backscattering ($r \sim 0.03$)

$$G / G_0 = 1 - 2r^2 \left[1 + \eta \cos \left(2\pi \frac{AB}{\Phi_0} \right) \right]$$

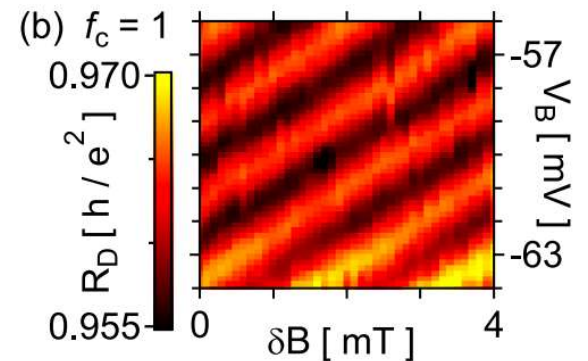
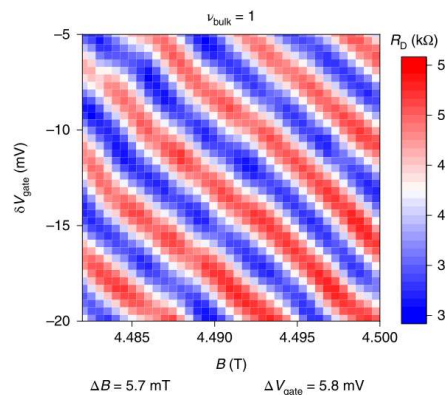
r = QPC reflectivity
 η = coherence factor
 A = interference Area
 Φ_0 = Flux quantum (h/e)

Interferometry regime

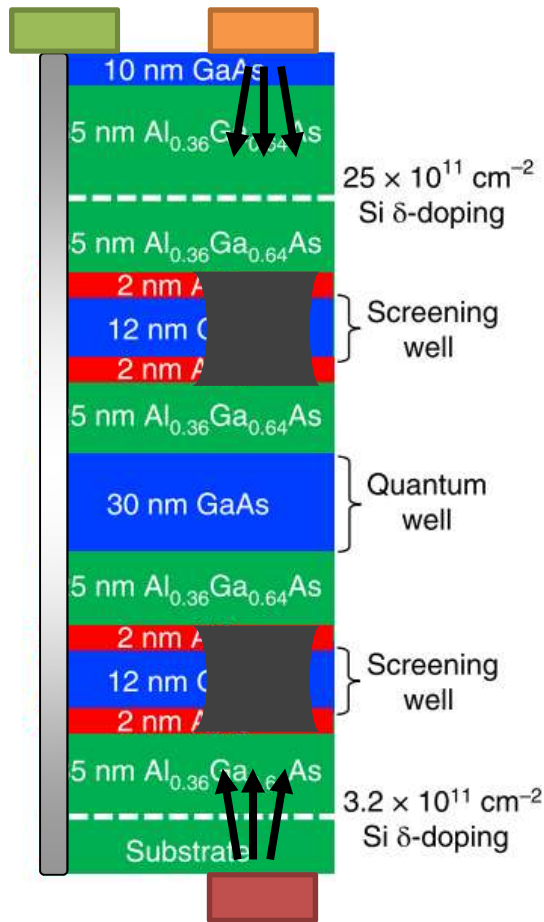
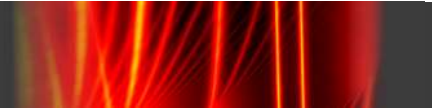


Aharonov-Bohm

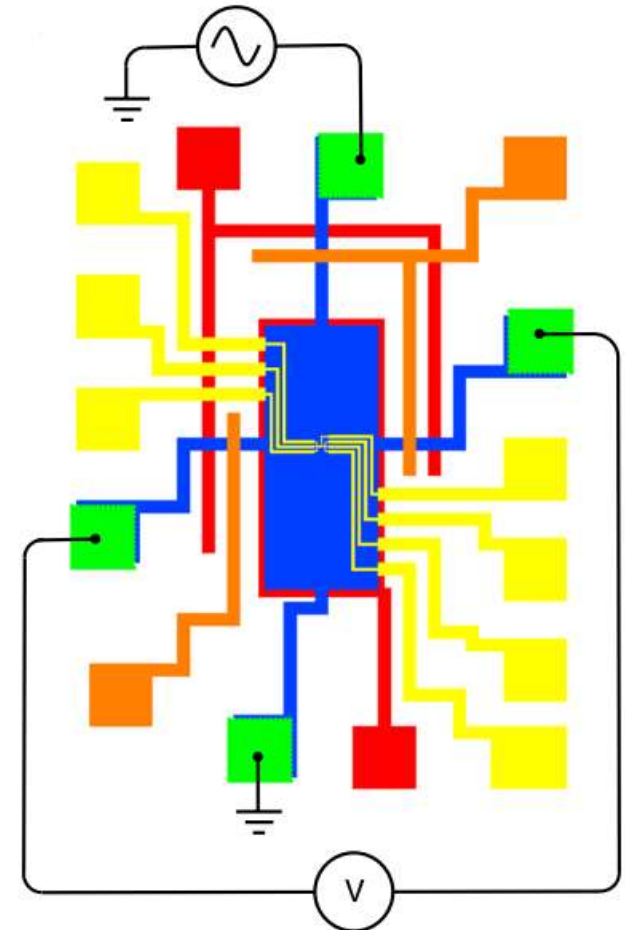
Coulomb Dominated

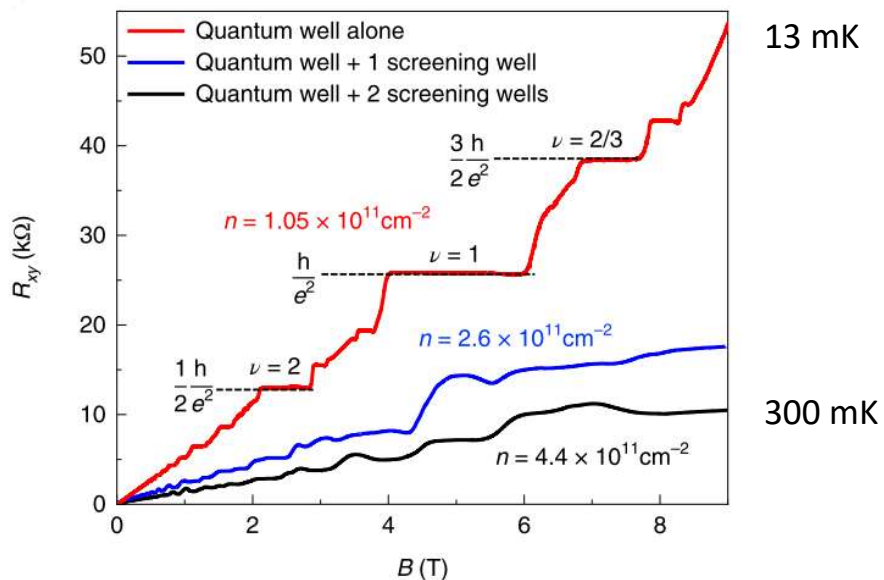


Halperin, B. et al. Phys. Rev. B 83, 155440 (2011).
 McClure, D. T. et al. Phys. Rev. Lett. 108, 256804 (2012).

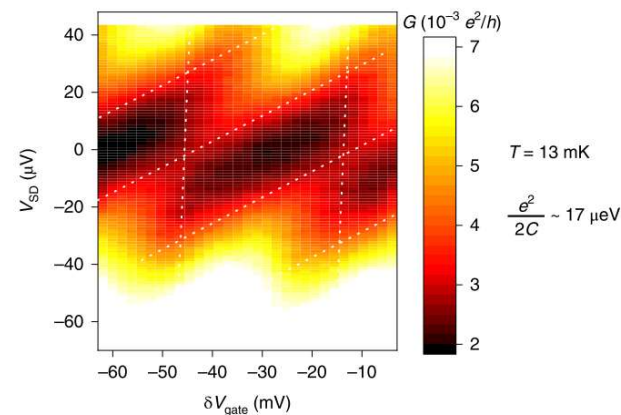


Ohmic contacts (green)
 Top gates (orange)
 Back gates (red)

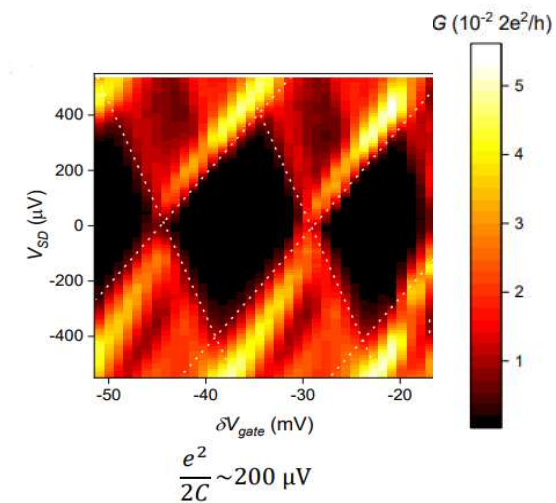


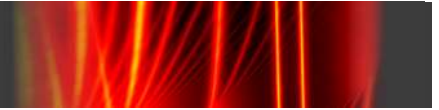


With screening wells



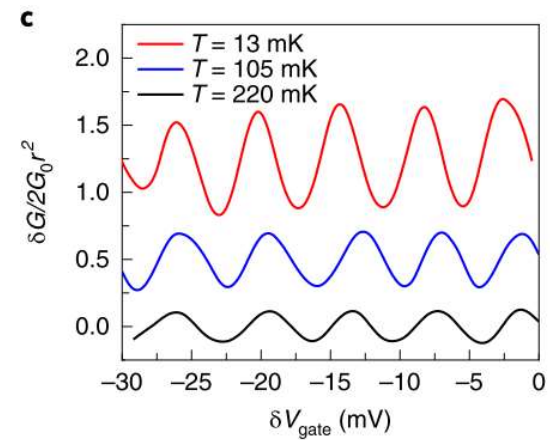
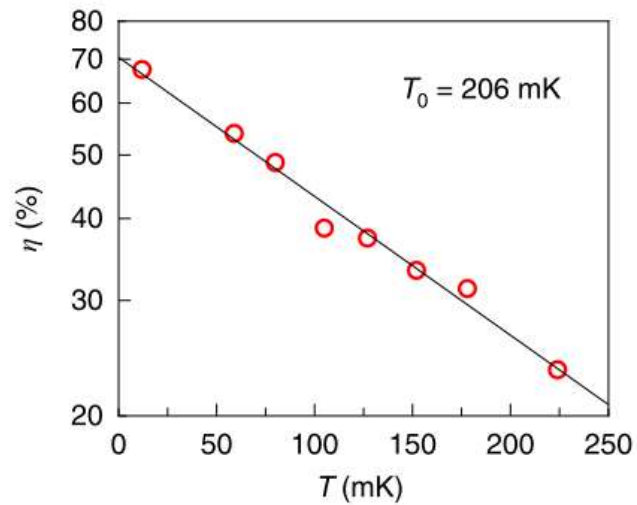
Without screening wells

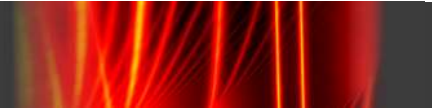




coherence factor η

- Amplitude of normalized $\nu=1$ oscillations

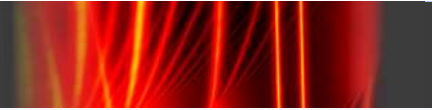




| | Nakamura (2019) | Meclure (2009) | Meclure (2012) | Willet (2013) | Rouleau (2008) | |
|---|--------------------|-------------------|-------------------|---------------------------------|-------------------|--|
| Area (μm^2) | 0.7 | 17 | 2 | 0.1-0.6 | | |
| E_C (μeV) | 17 | - | (25) | - | | |
| T_0 (mK) | 206 | - | 32 | - | 40 | |
| Mobility ($10^6 \text{ cm}^2 / \text{sV}$) | 7 | 20 | 20 | 28 | | |
| Density (10^{11} cm^{-2}) | 1.05 | 2.7 | 1.7 | 2.4/4.2 | | |
| Regime | AB | AB | CD | AB/CD | | |
| | | | | Depending on illumination | Mach- Zender | |

AB = Aharonov-Bohm

CD = Coulomb dominated



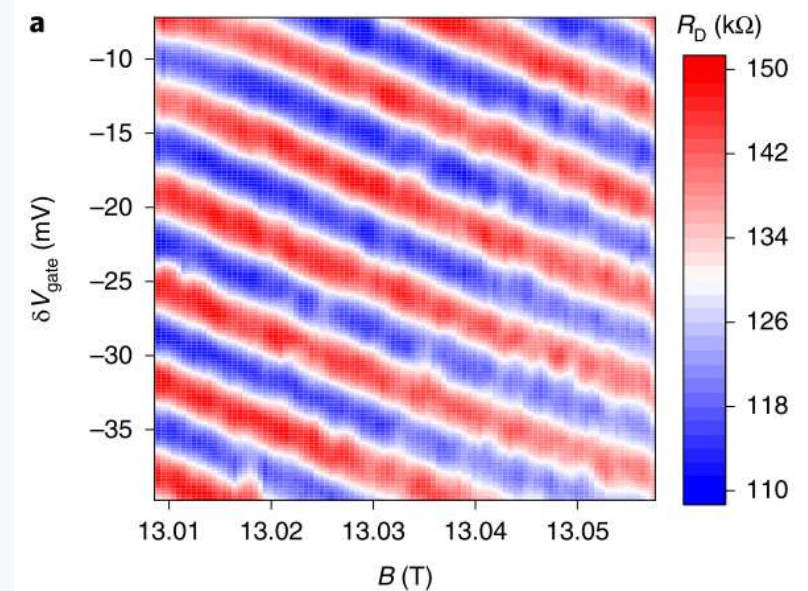
Modified AB-Phase

$$\theta = 2\pi \frac{e^*}{e} \frac{A_I B}{\Phi_0}$$

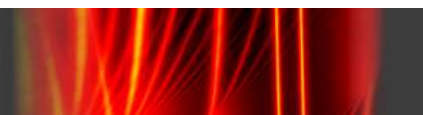
e^* fractional charge

- AB – interference of fractionally charged particles is observed
- No fractional braiding statistics
 - no expected phase jump $\Delta\theta_{\text{anyon}} = 4\pi/3$

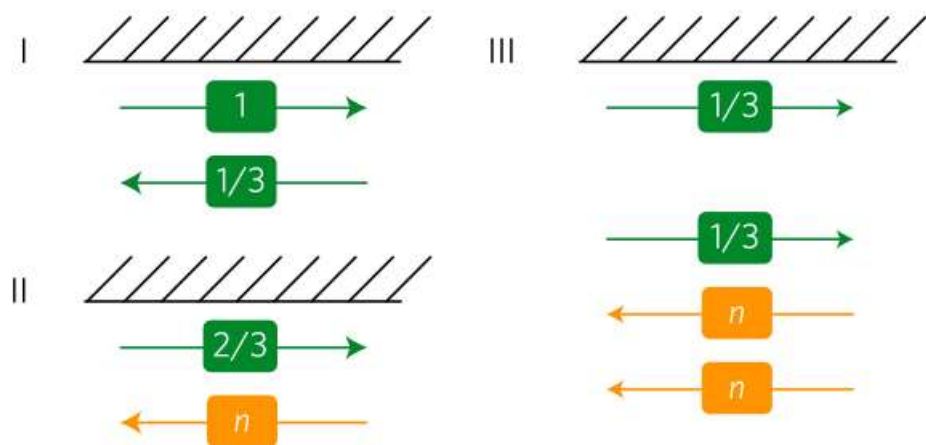
AB - interference of $\nu=1/3$ edge states



Charge fraction $e^*/e = 0.29$



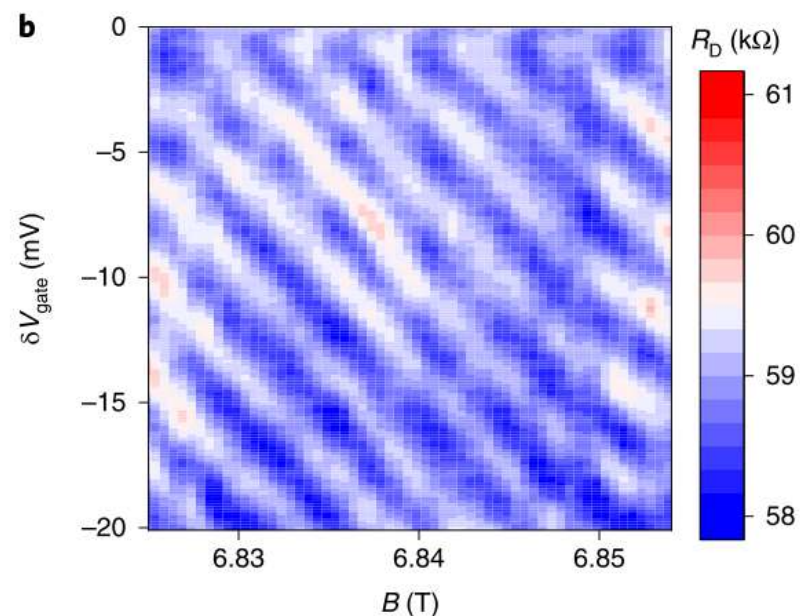
Possible realizations of $\nu=2/3$ edge states



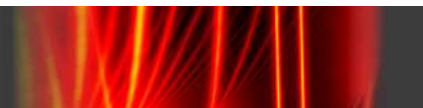
Possible evidence towards I (MacDonald edge structure)

Sabo R., Gurman I., *Edge reconstruction in fractional quantum Hall states*. Nature Physics volume13, pages491–496 (2017)

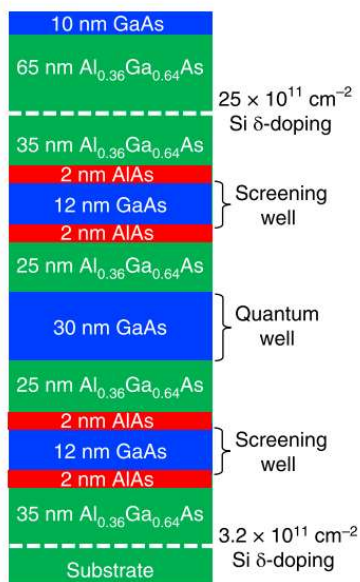
AB – interference of $\nu=2/3$ edge states



Measured charge fraction $e^*/e = 0.93$



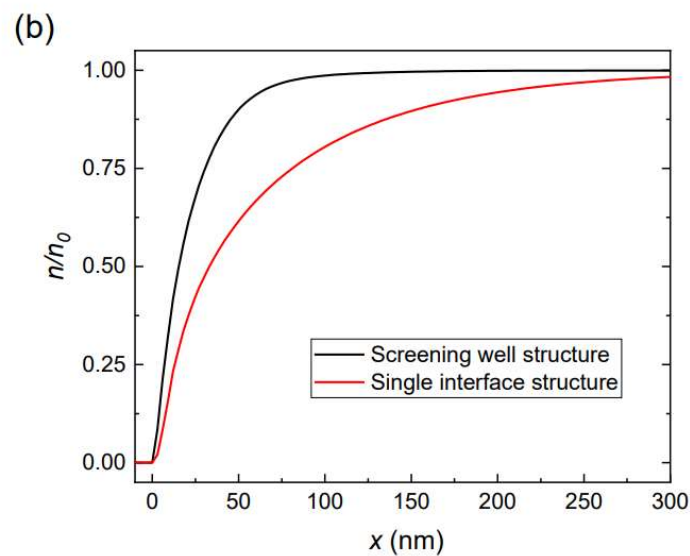
Steeper confinement potential may favor MacDonald structure



With screening wells

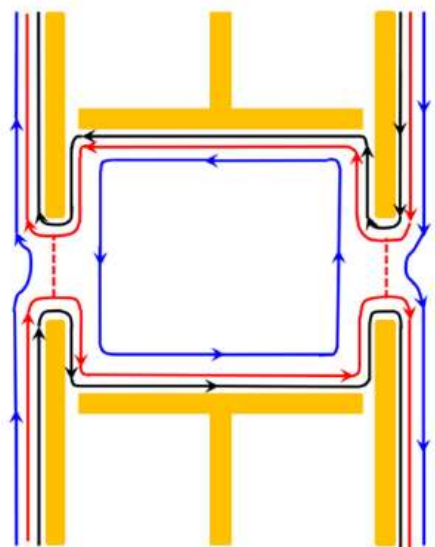
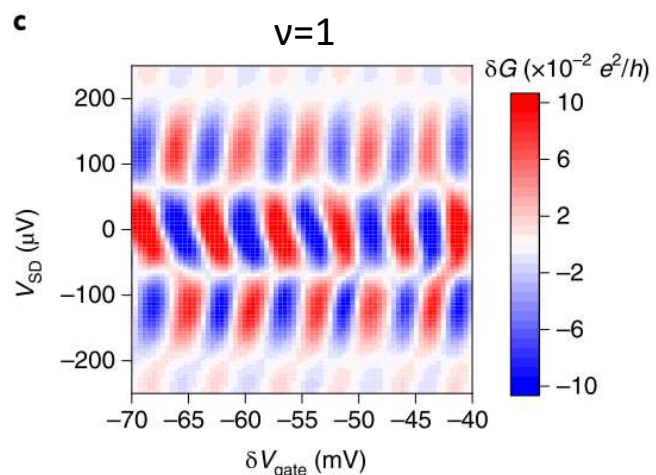
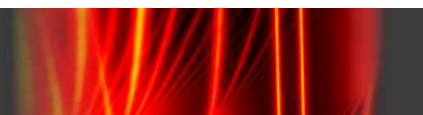


Without screening wells



Meir, Y. *Composite edge states in the $\nu = 2/3$ fractional quantum Hall regime*. Phys. Rev. Lett. 72, 2624–2627 (1993).

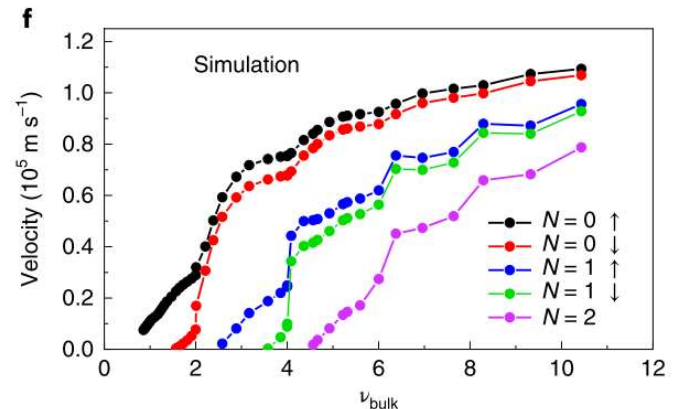
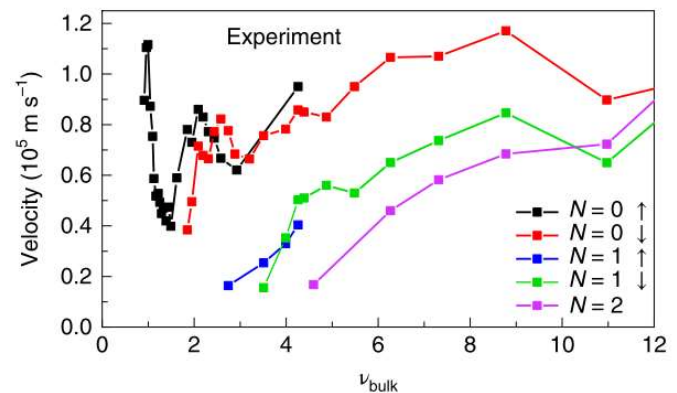
Edge state velocities

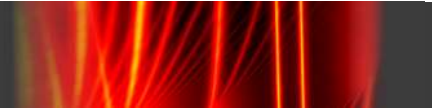


Completely backscattered
 Partially backscattered
 (interference)
 Completely transmitted

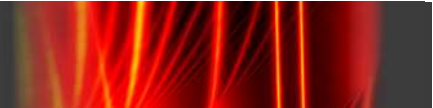
$$\delta G \propto \cos\left(2\pi \frac{AB}{\Phi_0}\right) \cos\left(\frac{eV_{SD}L}{2\hbar v_{edge}}\right)$$

$$v_{edge} = \frac{eL\Delta V_{SD}}{2\pi\hbar}$$





- Screening wells allow for AB - interferometry by screening coulomb interaction (despite lower density)
- Confirmation of fractional charge of $\nu=1/3$
- Hints of $\nu=2/3$ edge state structure where found
- Integer edge state velocities where investigated



Thank you
for your attention.